Effect of Thermal Properties of a Coated Elastohydrodynamic Lubrication Line Contact Under Various Slide-to-Roll Ratios

Huaiju Liu
State Key Laboratory of Mechanical Transmissions, Chongqing University, Shazhengjie 174, Chongqing 400044, China
E-mail: huaijuliu@cqu.edu.cn

Caichao Zhu
State Key Laboratory of Mechanical Transmissions, Chongqing University, Shazhengjie 174, Chongqing 400044, China
E-mail: cczhu@cqu.edu.cn

Zonglin Gu
State Key Laboratory of Mechanical Transmissions, Chongqing University, Shazhengjie 174, Chongqing 400044, China
E-mail: 1148752323@qq.com

Zhanjiang Wang
Department of Mechanical Engineering, Southwest Jiaotong University, Chengdu 610031, China
E-mail: wangzhanjiang001@gmail.com

Jinyuan Tang
State Key Laboratory of High Performance Complex Manufacturing, Central South University, Changsha 410083, Hunan, China
E-mail: jytangcsu@163.com

Zonglin Gu
State Key Laboratory of Mechanical Transmissions, Chongqing University, Shazhengjie 174, Chongqing 400044, China
E-mail: 1148752323@qq.com

Jinyuan Tang
State Key Laboratory of High Performance Complex Manufacturing, Central South University, Changsha 410083, Hunan, China
E-mail: jytangcsu@163.com

A numerical thermal elastohydrodynamic lubrication (EHL) model is developed for coated line contacts by considering both the mechanical properties and the thermal properties of the coating and the substrate. The temperature fields within the oil film and within the solids are solved by deriving the energy equations for the solids and the oil film. Heat continuity conditions are satisfied at the interfaces between the solids and the oil film, and the coating/substrate interfaces. Effects of the slide-to-roll ratio (SR), the thermal conductivities of the coating bodies, and the oil film on temperature fields are studied.

[DOI: 10.1115/1.4036078]

Introduction

Coatings are extensively applied in engineering, such as surfaces of gear tooth, cams and bearings, etc., due to their good tribological performance [1–4]. The usage of coating on engineering surfaces aims at either the reduction of the friction and wear or the improvement of surface durability. Theoretical studies on the tribological effect of coatings started from the cases of rigid substrates bonded to elastic coatings such as those shown in Refs. [3,6]. Recently, the frequency response functions, relating the contact pressure to the surface displacement and stress components, derived from the Papkovich–Neuber potentials, have been used for the calculation of multilayer contact problems by Wang et al. [7]. However, most coated contact studies assumed the isothermal condition and attentions were mainly paid to the effects of the rigidity and the thickness of the coating on the pressure and the film thickness during contacts [8]. Under a lubricated sliding-while-rolling condition with heavy normal load, the shear stress within the oil film, due to the relative motion between the two interacting surfaces, causes significant temperature rise within the contact area. The temperature rise changes the viscosity and the shear stress of the lubrication film, which further affects the frictional behavior and the surface failure behavior such as scuffing. Björing et al. [9] concluded that the significantly reduced friction in the diamond-like carbon (DLC)-coated EHL contact was mainly due to the thermal phenomenon. The consideration of the thermal effect in a lubricated contact problem leads to the coupling of the temperature field and the pressure field within the contact zone and a thermo-lubrication model is often required. Yang et al. [10] developed a thermo-elastohydrodynamic lubrication (TEHL) model to solve contact problems. However, most thermal lubrication models are limited to uncoated contact cases.

Generally, the coating and the substrate materials differ not only in the mechanical properties such as the Young’s modulus and the Poisson’s ratio but also in the thermal properties such as the heat capacity and the thermal conductivity. The thermal conductivity of the steel frequently used as the substrate material in engineering is approximately 30–50 W/(m K), while Liu et al. [11] suggested that the thermal conductivity of the DLC coatings was in the range of 0.7–7 W/(m K) depending on the film composition and the structure. In a general contact problem, the differences in the thermal properties between the coating, the substrate and the oil film affect the tribological performance which is yet to be discovered. This work studies the effects of the thermal properties of the solids and the oil film such as the thermal conductivity and the heat capacity on the tribological performance of a coated EHL line contact by developing a numerical thermal-elastohydrodynamic lubrication model which considers the differences in the mechanical and thermal properties between the coating and the substrate. The energy equations of the oil film, the coating, and the substrate are derived, respectively. The generalized Reynolds equation, first proposed by Yang and Wen [12], is applied to incorporate the effect of the Ree-Eyring non-Newtonian fluid behavior and the thermal effect on the pressure distribution. The two-dimensional frequency response function derived in Ref. [13], relating the pressure to the surface displacement, is utilized in combination with the discrete convolute, fast Fourier transform (DC-FFT) method [14] to incorporate the effect of mechanical properties of the coating.

Methodology

The lubricated line contact between two smooth coated rollers is studied, which is a suitable simplification of many engineering applications such as the contact of the spur gear tooth or the roller bearing. It is easy to further incorporate the surface roughness in the model; however, the roughness is ignored in this current work. The two coated rollers (solids a and b) are rolling with their own rolling velocities under an external normal load $F$ (unit N/m), as shown in Fig. 1. The thermal properties as well as the mechanical properties of the substrates, the coatings, and the oil film are listed in the figure.

The governing energy equations for the oil film and the solids are different from each other, and therefore along the $z$ direction, representing the direction of the normal load, the film and the solids are treated separately, as shown in Ref. [15]. The energy equation of the oil film can be expressed as

\[ F_z = \frac{\partial P}{\partial z} + \rho \frac{\partial^2 u_z}{\partial t^2} \]

where $F_z$ is the normal load force, $P$ is the pressure, $\rho$ is the density of the oil film, and $u_z$ is the vertical displacement of the film surface.
The generalized Reynolds equation, considering the variation of the velocity of the fluid across the film thickness, is applied and detailed expression can be found in Ref. [17]. The elastic deformation is calculated using the DC-FFT method with the influence coefficient obtained through the frequency response function, which relates the pressure to the surface displacement [18]. The Roelands viscosity–pressure–temperature relation [19] and the Dowson and Higginson density–pressure relation [20] are applied to describe the viscosity and the density of the fluid, respectively.

The dimensionless form and the discretization scheme are available in Ref. [15]. The coefficient matrix of the set of governing equations of the temperature field can be written as a tridiagonal matrix which is diagonally dominant. This set of equations can be solved efficiently with the chasing method. In this work, 1029 equally spaced nodes are arranged along the rolling direction within the calculation domain $X_i \in [-4, 3] (i = 0, 1, \ldots, 1024)$. The convergence criteria of the pressure $P$, the natural load $\sum |P| |\Delta X|$, and the temperature $T$ at any transient time step are chosen as $\sum |P - P_i|/\sum |P| < 0.00001$, $|\sum |P| |\Delta X| - (\pi/2)|/\pi < 0.00001$, and $\sum |\sum |T_j - T_{1j}|/\sum |T_{1j}| < 0.00001$, respectively, where $P_i$ is the updated dimensionless pressure and $P$ is the old dimensionless pressure value, $T_{1j}$ is the updated dimensionless temperature and $T_{1j}$ is the old dimensionless temperature before the current iteration.

Results and Discussion

The working conditions and properties of the lubricant and the solids are listed in Table 1. The mechanical properties of the substrate materials of solids a and b are kept the same. The coating thickness of solids a and b is identical with each other. A large range of the slide-to-roll ratio SR $\in [0.1, 2.0]$ is selected to represent common conditions occurring in engineering applications such as gear drives. The thermal properties such as the thermal conductivity, the heat capacity of the solids, and of the oil are manually changed within a large range to show their effects on the tribological performance of the lubricated contact.

The effect of mechanical properties, i.e., the rigidity and the thickness of the coating, on the pressure and the film thickness has already been studied in Refs. [21–23]. The current model is validated through the comparison of the pressure profile and the film thickness with previous results.

The slide-to-roll ratio is an important parameter affecting the tribological behavior of the contact bodies. Not only the surface failure mechanism is affected but also the friction and the temperature rise are influenced by the slide-to-roll ratio significantly. Figure 2 shows the effect of slide-to-roll ratio on the temperature profile at five characteristic layers along the normal load direction, i.e., the coating/substrate (C/S) interfaces and the surfaces of the two solids and the central oil film layer, under the working condition $F = 5 \times 10^5$ N/m, $u_i = 1$ m/s, $E_c = 2E_a$, $h_i = 100 \mu$m, $h_i = 100 \mu$m.
The solids under three slide-to-roll ratios, i.e., SR = 0.1–2.0.

When the slide-to-roll ratio changes, the temperature at each layer varies consequently. The variations at the central oil film layer, the surface of solid b and its C/S interface are significant, while those at the surface of solid a and its C/S interface are negligible. Difference of the temperature variations at the central oil film layer, the surface of solid b and its C/S interface are significant, while those at the surface of solid a, i.e., \( u_a > u_b \), while the rolling speed of the contact \( u_r \) is kept constant, and results are shown in Fig. 4.

As a comparison, the sign of the sliding velocity is changed by making the rolling velocity of the surface of solid b larger than that of the surface of solid a, i.e., \( u_b > u_a \), while the rolling speed of the contact \( u_r \) is kept constant, and results are shown in Fig. 4.

Figure 3 shows the whole temperature field within the oil film and the solids under three slide-to-roll ratios, i.e., SR = 0.424, 1.144, 1.864. It shows clearly that the temperature rise inside the oil film increases significantly as the slide-to-roll ratio increases. The maximum temperature rise increases from 5% for the case SR = 0.424 to 21% for the case SR = 1.864. Under the latter case, the highest temperature within the contact reaches 380 K. Since there is a sliding velocity between the surfaces of the two solids, the location of the maximum temperature rise shifts from the central oil film layer to the surface of solid b, which has a smaller rolling speed compared with the surface of solid a.

As a comparison, the sign of the sliding velocity is changed by making the rolling velocity of the surface of solid b larger than that of the surface of solid a, i.e., \( u_b > u_a \), while the rolling speed of the contact \( u_r \) is kept constant, and results are shown in Fig. 4. As can be seen, the location of the maximum temperature rise shifts from the central oil film layer to the surface of solid a.
which has a smaller rolling speed. And this tendency becomes more clear as the slide-to-roll ratio increases.

Thermal conductivity is an important property for heat transfer. The thermal conductivity of a material represents the ability to transfer heat by conduction. Reference [21] defines two thermal conductivities $k_c = 5 \text{ W/mK}$ and $k_c = 90 \text{ W/mK}$ to investigate the effect of the thermal inertia. Figure 5 shows the detailed temperature distribution under three thermal conductivities of the coating, ranging from $k_c = 2.1 \text{ W/mK}$ to $k_c = 186.1 \text{ W/mK}$. The maximum temperature rise decreases from 360 K to 345 K, when the thermal conductivity of the coating increases from $k_c = 2.1 \text{ W/mK}$ to $k_c = 186.1 \text{ W/mK}$. The coating with a relatively low thermal conductivity prevents heat generated by the oil film shear action from being diffused from the center of the contact toward the peripheral area and the solids, which would lead to a high temperature rise within the center of the contact.

Effect of thermal conductivity of the oil is shown in Fig. 6 with three cases: $k_{oil} = 0.171, 0.283, 0.395 \text{ W/mK}$. As the thermal conductivity of the oil increases from $k_{oil} = 0.171 \text{ W/mK}$ to $k_{oil} = 0.395 \text{ W/mK}$, the maximum temperature rise within the contact area decreases from 350 K to 335 K. The temperature rise mainly occurs at the center of the Hertzian contact region, and the
temperature within the oil film is much higher than that within the solids. The high ability of the oil to conduct heat assists the heat diffusing to the peripheral area and the solids, which further leads to the reduction of the temperature within the oil film. The increase of the thermal conductivity of the coating and of the oil film is helpful for the restraint of the temperature rise during contact.

Conclusion

Effect of the thermal properties of a coated EHL line contact is studied by emphasizing the difference between the thermal properties of the coating and of the substrate. Heat continuity conditions are satisfied at the surfaces of the solids and the coating/substrate interfaces. The maximum temperature rise increases from 5% for the case with slide-to-roll ratio $SR = 0.424$ to 21% for the case with $SR = 1.864$. The direction of the sliding velocity causes the difference in temperature between the two surfaces of solids. The temperature of the surface with the smaller rolling velocity is higher than that of the surface with the larger rolling velocity. The maximum temperature rise decreases from 360 K to 345 K when the thermal conductivity of the coating increases from $k_c = 2.1 \text{ W/m K}$ to $k_c = 186.1 \text{ W/m K}$. The coating with a relatively low thermal conductivity prevents heat generated by the oil film shear action from being diffused from the center of the contact toward the peripheral area and the solids, which would lead to a high temperature rise within the center of the contact. As the thermal conductivity of the oil increases from $k_{oil} = 0.171 \text{ W/m K}$ to $k_{oil} = 0.395 \text{ W/m K}$, the maximum temperature rise within the contact area decreases from 350 K to 335 K.

Acknowledgment

This work is financially supported by the National Natural Science Foundation of China (Grant Nos. 51405042, 51535012, and 51575061) and the China Postdoctoral Science Foundation (Grant No. 2015M582516).

Nomenclature

- $b_0$ = the Hertzian contact half-width under the uncoated case, m
- $c_o$, $c_s$ = heat capacity of the coating material, J/kg K
- $c_{oil}$ = heat capacity of the substrate material, J/kg K
- $d$ = the depth at the bottom boundary of the calculational domain, m
- $E_c$ = Young’s modulus of the coating, Pa
- $E_s$ = Young’s modulus of the substrate, Pa
- $F$ = the normal load, N
- $h_{oil}$, $h_{b}$ = coating thickness of the two solids a and b, respectively, m
- $I$ = all variables should appear in italics
- $k_c$ = thermal conductivity of the coating material, W/m K
- $k_s$ = thermal conductivity of the substrate material, W/m K
- $k_{oil}$ = thermal conductivity of the oil, W/m K
- $p$ = the contact pressure, Pa
- $R_a$, $R_b$ = radius of curvature of the two solids a and b, respectively, m
- $SR$ = the slide-to-roll ratio
- $T_0$ = ambient temperature and the inlet oil temperature, K
- $u_r$ = the rolling speed, m/s
- $\nu$ = the Poisson’s ratio of materials
- $\eta$ = the pressure–viscosity coefficient, Pa$^{-1}$
- $\eta_{oil}$ = current oil viscosity, Pa $\cdot$ s
- $\rho_c$ = oil viscosity at ambient pressure, Pa $\cdot$ s
- $\rho_o$ = density of the coating material, kg/m$^3$
- $\rho_s$ = density of the substrate material, kg/m$^3$
- $\rho_{oil}$ = the density of the oil, kg/m$^3$
- $\eta_{oil}$ = the ambient density of the oil, kg/m$^3$
- $G_0$ = the Eyring characteristic stress, Pa

References